Year 13 Mathematics Mock Set#04d Pure Paper 1

Year 13 revision session 2023

- Advised to print in "A3-booklets", this will allow all questions to be on the left hand side.
- You can also print in A4, double-sided, and two staples on the left
- If instead you print in 2-in-1 settings, first print the second page up to the last page, then print the cover page separately (to allow all questions on the left)

This exam paper has 14 questions, for a total of 100 marks.

Question	Marks	Score
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Total:	100	

Andrew Chan

Last updated: 5th June 2023

- 1. Mr Chan reports the number of visits of SoHokMaths at the end of each month from September 2022. He believes that the relationship between the number of visits, n, and the number of months after the start of the academic year, t, can be modelled by $n = a \times 2^{kt}$ where a and k are constants.
 - (a) Show that, according to the model, the graph of $\log_{10} n$ against t is a straight line.

(2)

(b) Figure 1 shows a plot of the values of t and $\log_{10} n$ from September 2022, the point at t = 1, to March 2023, the point at t = 7.

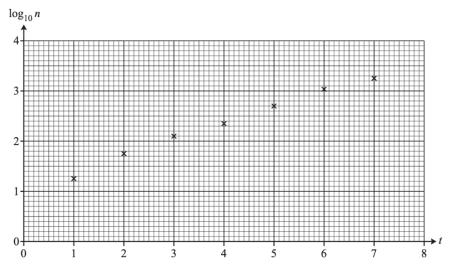


Figure 1

Find estimates of the values of a and k.

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(Total for Question 1 is 6 m	

2.	Given that $\mathbf{v} = 2\mathbf{a} + 3\mathbf{b}$, where \mathbf{a} and \mathbf{b} are position vectors $\mathbf{a} = \begin{pmatrix} 5 \\ 3 \end{pmatrix}$ and $\mathbf{b} = \begin{pmatrix} -1 \\ 6 \end{pmatrix}$.	
	(a) Determine the magnitude of \mathbf{v} .	(9)
	(1)	(3)
	(b) Determine the angle between \mathbf{v} and the vector $\begin{pmatrix} 1 \\ 0 \end{pmatrix}$.	
		(2)

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Question 2 continued	
(To	tal for Question 2 is 5 marks)

3.	(a)	Prove	the	identity
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$$\frac{\sin^3 \theta}{\sin \theta - 1} - \frac{\sin^2 \theta}{1 + \sin \theta} \equiv -\tan^2 \theta (1 + \sin^2 \theta)$$

(4)

(b) Hence solve the equation

$$\frac{\sin^3 \theta}{\sin \theta - 1} - \frac{\sin^2 \theta}{1 + \sin \theta} = \tan^2 \theta (1 - \sin^2 \theta)$$

for $0 < \theta < 2\pi$

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	$\theta = \arcsin x$	
	(a) By expressing $\arccos x$ in terms of θ , show that	
	$\arcsin x + \arccos x = \frac{\pi}{2}$	
		(3)
	(b) Hence or otherwise solve the equation	(0)
	(b) Hence, or otherwise, solve the equation	
	$3\arcsin(y-1) = 2\arccos(y-1)$	
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5. Four students, Tom, Andrew, Zakiyyah, Maria are attempting to complete the indefinite integral

$$\int \frac{1}{x} \, \mathrm{d}x \qquad \{x > 0\}$$

Each of the students' solutions is shown below:

Tom
$$\int \frac{1}{x} \, \mathrm{d}x = \ln x$$

Andrew
$$\int \frac{1}{x} \, \mathrm{d}x = k \ln x$$

Zakiyyah
$$\int \frac{1}{x} \, \mathrm{d}x = \ln Ax$$

Maria
$$\int \frac{1}{x} \, \mathrm{d}x = \ln x + c$$

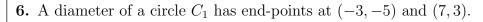
- (a) Tom and Andrew are both incorrect.
 - (i) Explain what is wrong with Tom's answer.
 - (ii) Explain what is wrong with Andrew's answer.

(2)

(b) Zakiyyah and Maria are both correct, explain why their answers are equivalent.
(2)

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Question 5 continued				
(Total for Question 5 is 4 marks)				



(a) Find an equation of the circle C_1 .



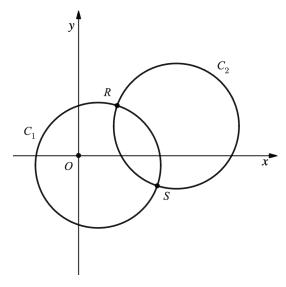


Figure 2: https://www.desmos.com/calculator/a0zitxwiir

The circle C_1 is translated by $\binom{8}{4}$ to give circle C_2 , as shown in Figure 3.

(b) Find an equation of the circle C_2 .

(2)

The two circles intersect at points R and S.

(c)	Show tha	t the	equation	of the	line RS	is $y =$	-2x + 13.
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Question 6 continued	
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$$f(x) = 2x + 3 \qquad \text{for } x < 0$$

$$g(x) = x^2 - 2x + 1$$
 for $x > 1$

(a) Find gf(x), stating the domain.

(3)

(b) State the range of gf(x).

(1)

(c) Find $(gf)^{-1}(x)$

Note here that even though question did not specify, you always need to state the domain for any functions you "found"

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stion 7 continued	
	(Total for Question 7 is 9 ma

8. A student of Mr Chan, Diogo, is proving that

 $n^3 - n$ is a multiple of 3 for all positive integer values of n.

Diogo begins a proof by exhaustion.

- Diogo's response ———

Step 1
$$n^3 - n = n(n^2 - 1)$$

Step 2 When
$$n = 3m$$
, where m is $n^3 - n = 3m(9m^2 - 1)$ a non-negative integer which is a multiple of 3

Step 3 When
$$n = 3m + 1$$
, $n^3 - n = (3m + 1)((3m + 1)^2 - 1)$

Step 4
$$= (3m+1)(9m^2)$$
$$= 3(3m+1)(3m^2)$$
which is a multiple of 3

Step 5 Therefore $n^3 - n$ is a multiple of 3 for all positive integer values of n.

(a) Explain the two mistakes that Diogo has made after Step 3.

(2)

(b) Correct Diogo's argument from Step 4 onwards.

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Question 8 continued	
	(Total for Question 8 is 6 marks)

- 9. Note that for Edexcel questions, (i) and (ii) means two unrelated questions, they are combined into one because they belong to the same chapter/topic.
 - (i) The first four terms of a sequence are 2, 3, 0, 3 and the subsequent terms are given by $a_{k+4} = a_k$.
 - (a) State what type of sequence this is.

(1)

(b) Find
$$\sum_{k=1}^{200} a_k$$
.

(1)

- (ii) A different sequence is given by $u_n = b^n$ where b is a constant and $n \ge 1$.
 - (a) State the set of values of b for which this is a divergent sequence.

(2)

(b) In the case where $b = \frac{1}{3}$, find the sum of all the terms in the sequence.

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10.	(a)	Find the first three terms in the binomial expansion of
		$\frac{2-x}{\sqrt{1+3x}}$
		in ascending powers of x .
		(5)
	(b)	State the range of values of x for which the expansion is valid.
		(1)
	(c)	By writing $x = \frac{1}{22}$ in your expansion, find an approximate value for $\sqrt{22}$ in the form $\frac{a}{b}$, where a and b are integers to be found.
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Question 10 continued	
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	(Total for Question 10 is 8 marks)

1.	The variables x and y satisfy the differential equation
	$\frac{\mathrm{d}y}{\mathrm{d}x} = \frac{xy}{1+x^2}$
	and $y = 2$ when $x = 0$.
	Solve the differential equation, obtaining a simplified expression for y in terms of x . (7

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12. The curve C is defined for $t \ge 0$ by the parametric equations

$$x = t^2 + t \qquad y = 4t^2 - t^3$$

A sketch of C is shown in Figure 4 below.

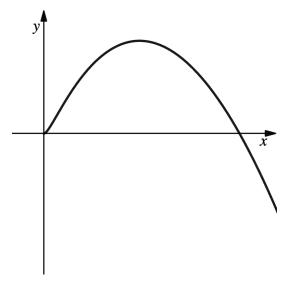


Figure 3: https://www.desmos.com/calculator/qbyvqlaoh3

(a) Find the gradient of C at the point where it intersects the positive x-axis.

(5)

The area A enclosed between C and the x-axis is given by

$$A = \int_0^b y \, \mathrm{d}x$$

(b) State the value of b.

(1)

(c) Use parametric integration to show that

$$A = \int_0^c \left(4t^2 + 7t^3 - 2t^4 \right) dt$$

where c is an integer to be found.

(3)

(d) Find the value of A.

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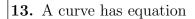
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$$y = a\sin x + b\cos x$$

where a and b are constants.

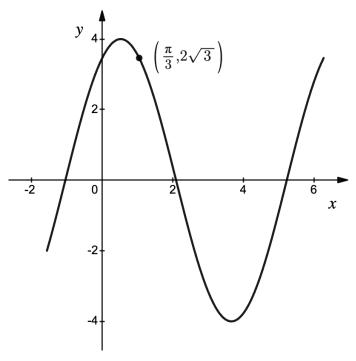


Figure 4: https://www.desmos.com/calculator/yq7kymbzzj

The maximum value of y is 4 and the curve passes through the point $\left(\frac{\pi}{3}, 2\sqrt{3}\right)$, as shown in Figure 5.

Find the values of a and b.

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14. (a) On Diagram 1 below, sketch on the same axes the graphs of $y = \frac{1}{x}$ and $y = \sec 2x$, hence show that the equation

$$\frac{1}{x} = \sec 2x$$

has exactly one solution for x > 0.

(3)

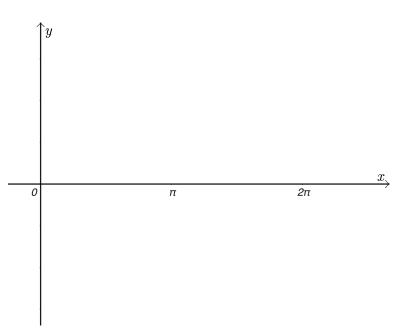


Diagram 1

(b) By considering a suitable change of sign, show that the solution to the equation lies between 0.4 and 0.6.

(2)

(c) Show that the equation in part (a) can be rearranged to give

$$x = \frac{1}{2}\arccos x$$

(2)

(d) Use the iterative formula

$$x_{n+1} = \frac{1}{2}\arccos x_n$$

with $x_1 = 0.4$, to find x_2 , x_3 and x_4 , giving your answer to four decimal places.

(2)

Question 14 continued

(e) On Diagram 2 below, draw a cobweb or staircase diagram to show how convergence takes place, indicating the positions of x_2 , x_3 and x_4 .

(2)

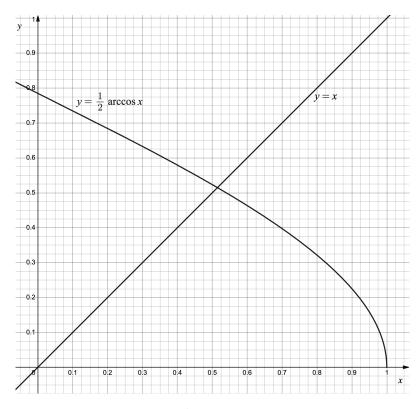


Diagram 2

Question 14 continued

Another copy of Diagram 1 if needed:

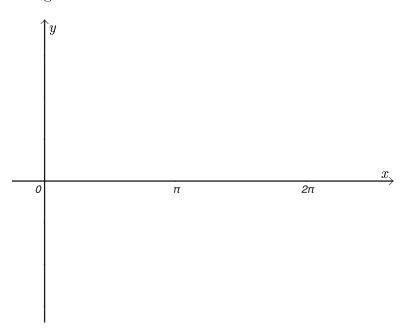


Diagram 1

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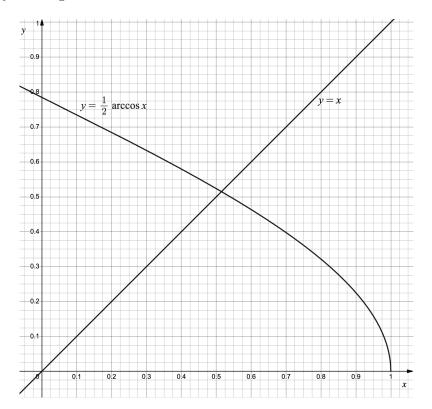


Diagram 2

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